

# Week 6-7: Wind-driven ocean circulation

Tally's book, chapter 7

# Recap so far...

- Our goal (since week 3) has been to **understand large-scale ocean circulation and its underlying physics, and to learn how to quantify them using available observations.**

# 1902



Fridtjof Nansen (1861-1930)



Vagn Walfrid Ekman (1874-1954)  
Univeristy of Lund



The Fram Expedition (Frist, 1893-1896)

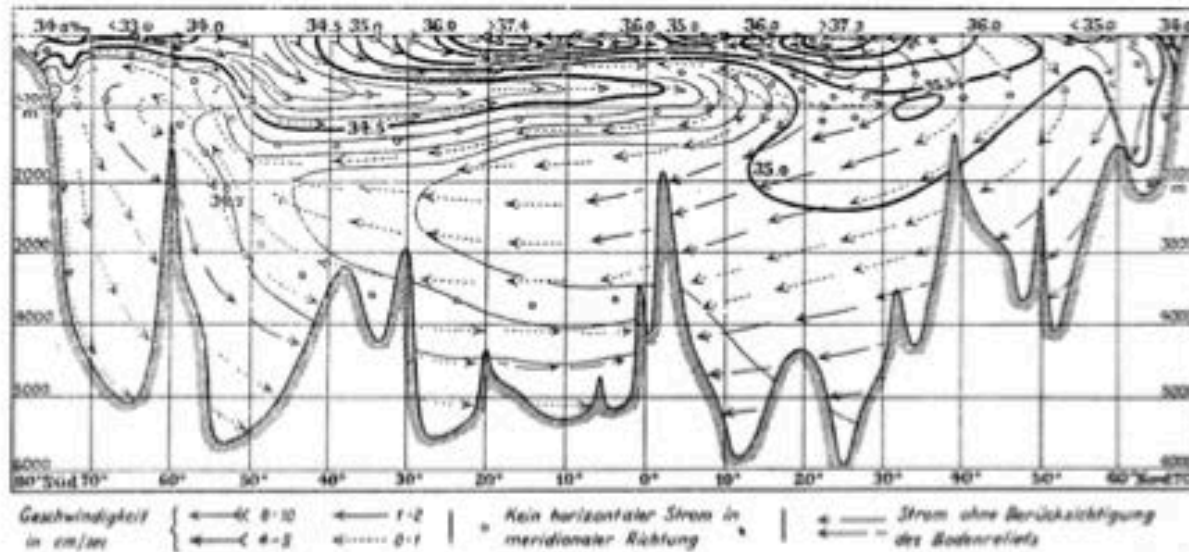
# Ekman flow

- Ekman circulation
  - Direct effect of wind on the surface current.
  - Balance of forces: Coriolis effect VS. wind stress
  - Ekman spiral (downward clockwise spiral in NH)
  - Ekman transport ( $90^\circ$  to the right of wind direction in NH)
  - Ekman layer : approx. top 20-30m of the ocean

# 1925

## Meteor expedition (1925-27)

- Testing the thermal wind balance
- Alfred Merz



Merz, 1925



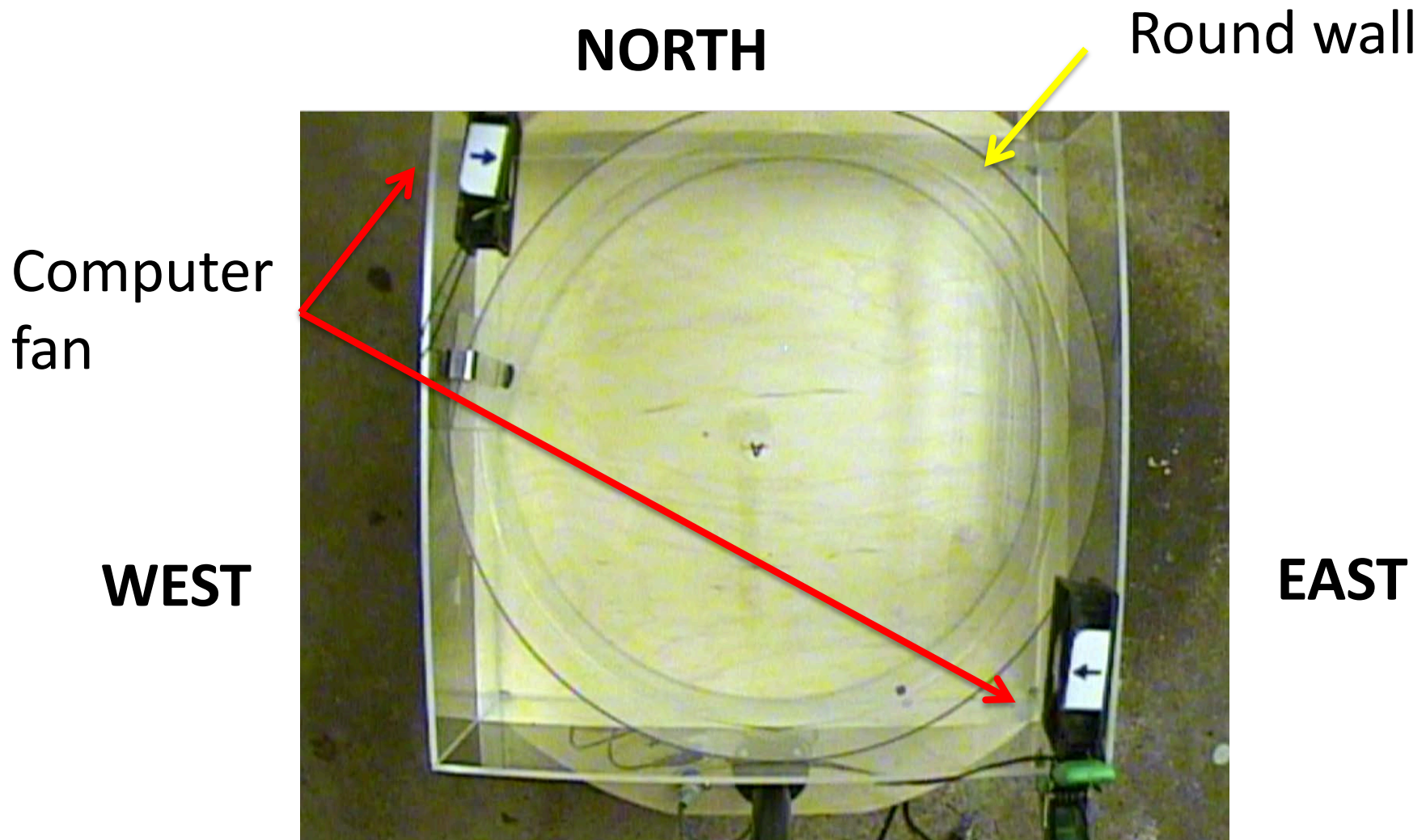
# Geostrophic flow

- Balance between Coriolis force and Pressure Gradient Force
- Use the “balance of forces” to determine ocean current speed and direction
  - Assume: frictionless and small Rossby number (slow speed, large-scale)
  - Cyclonic circulation (CCW in NH) around the low pressure
  - Anticyclonic circulation (CW in NH) around the high pressure

# Thermal wind

- Calculating geostrophic circulation using T-S measurements
  - YOU WANT: Horizontal current speed and direction
  - YOU NEED: Horizontal pressure gradient
  - AVAILABLE MEASUREMENT: T and S.
  - Use thermal wind relation: practically, we calculate dynamic topography → Steric sea level
    - Dynamic height is higher for the warmer water column
      - Anti-cyclonic flow in subtropics
    - Dynamic height is lower for the colder water column
      - Cyclonic flow in subpolar region
  - Level of no motion
    - We assume that the deep ocean is motionless ( $u=v=0$  in the deep ocean, say  $z=2,000\text{m}$ ) so we can apply thermal wind.
    - The velocity field you get from the dynamic topography is relative to the deep (e.g. 2000m) reference level.

# Tank experiment for Ekman flow



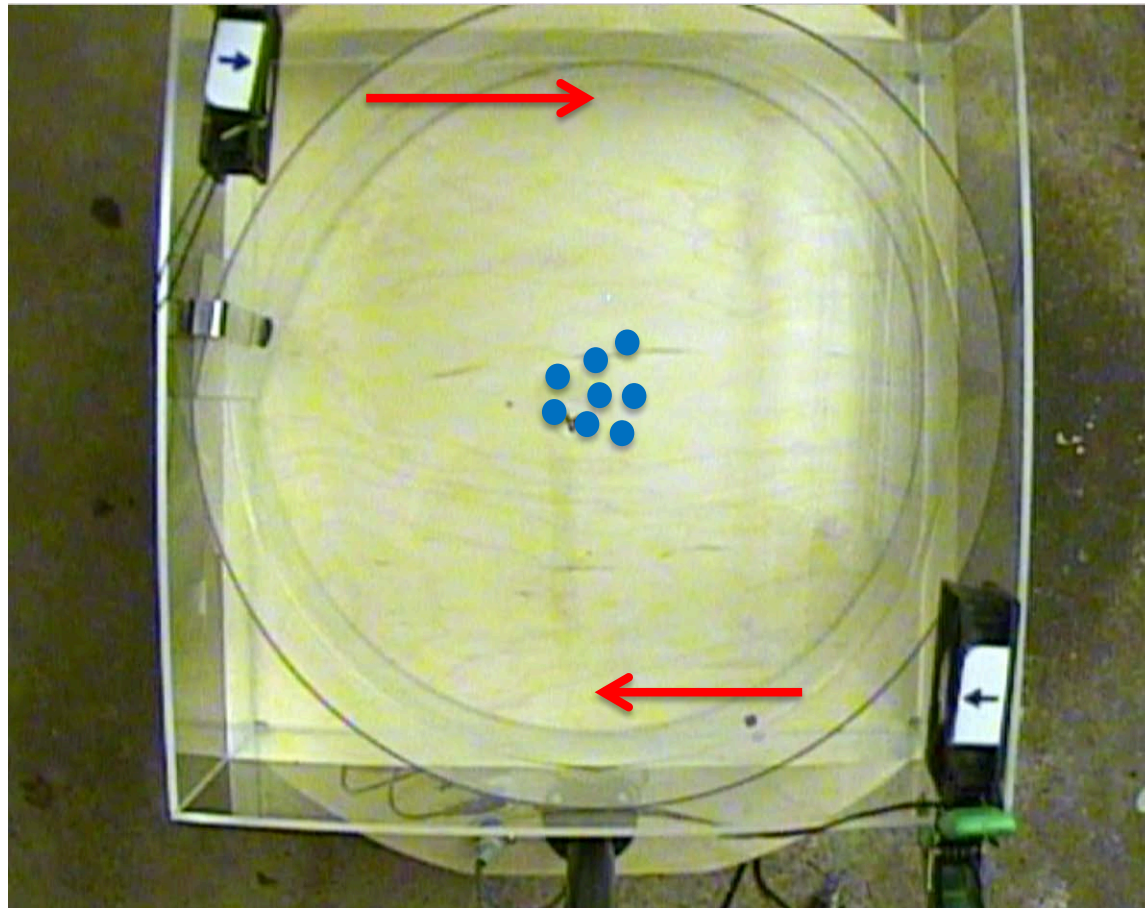
The view of the camera on top of the tank



The “anti-cyclonic” wind stress caused the surface Ekman flow to **converge** in the center

**NORTH**

Computer fan



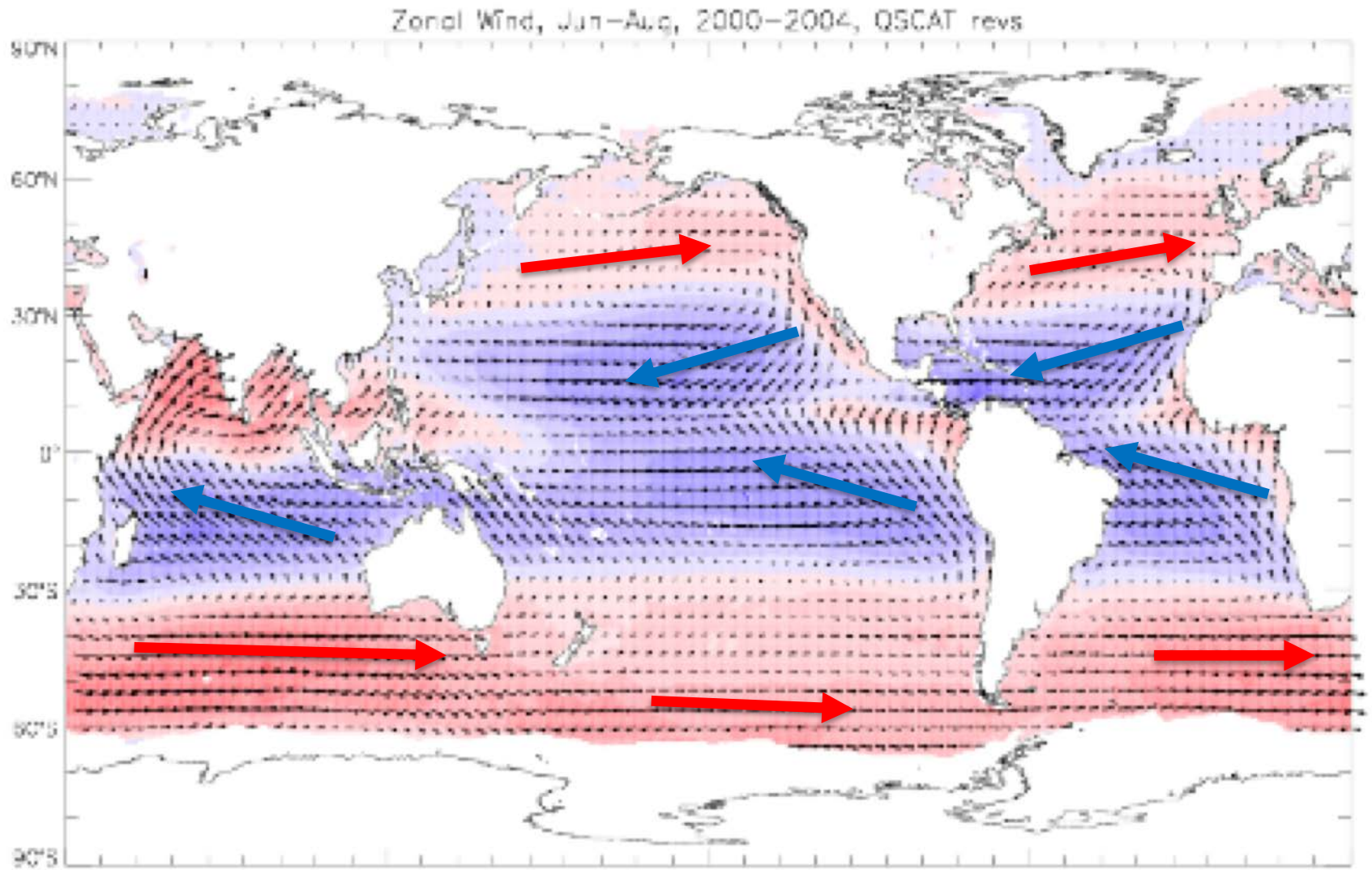
**WEST**

**EAST**

# Wind-driven vertical motion

- Cyclonic wind stress → Ekman upwelling
- Anti-cyclonic wind stress → Ekman downwelling (Ekman pumping)

# Observed wind stress



Blue = westward (trade wind)

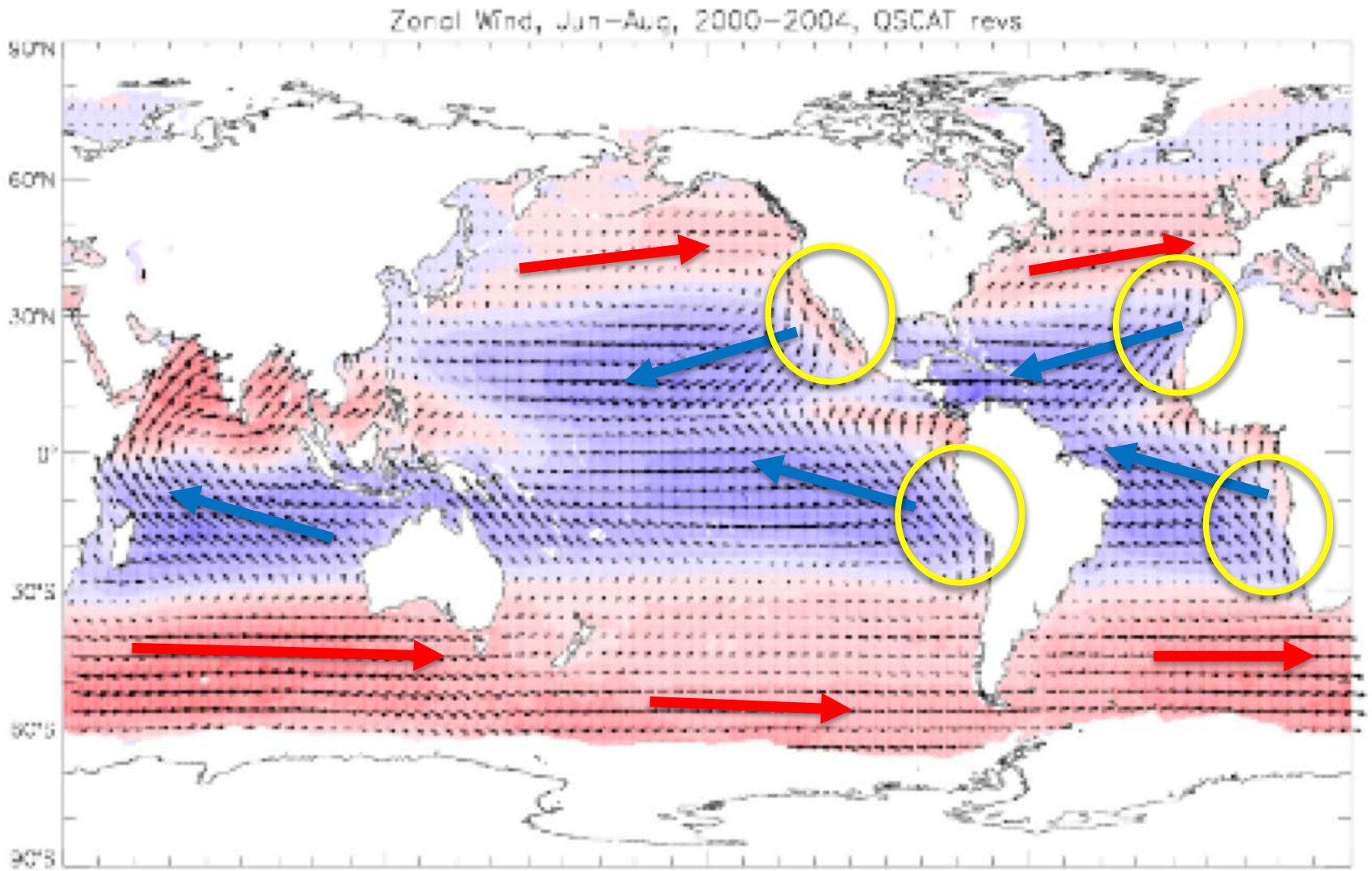
Red = eastward (westerly wind)

Cl = 2 m/s Min = -16.22 Max = 16.60





# Wind along the eastern boundary

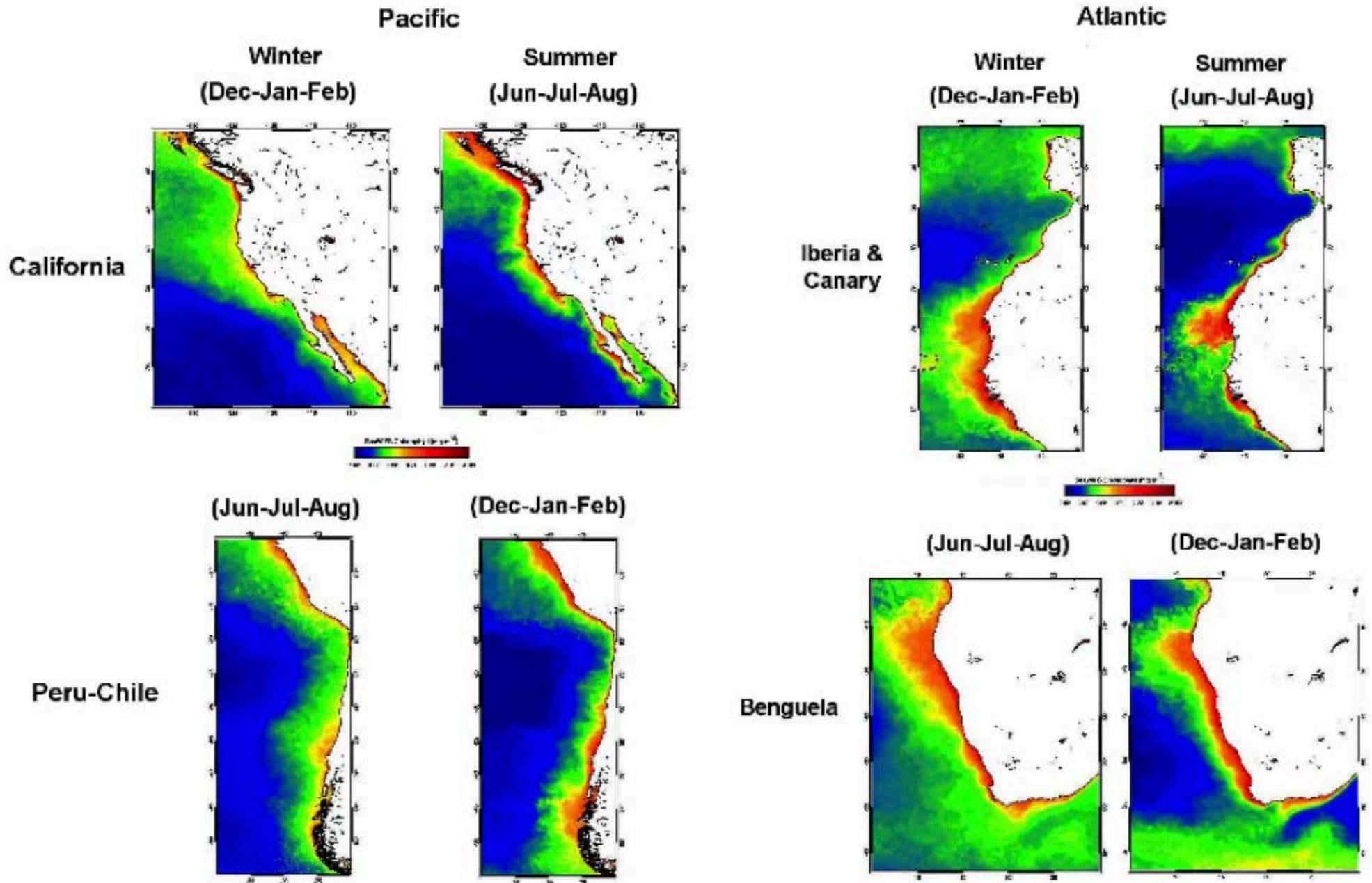


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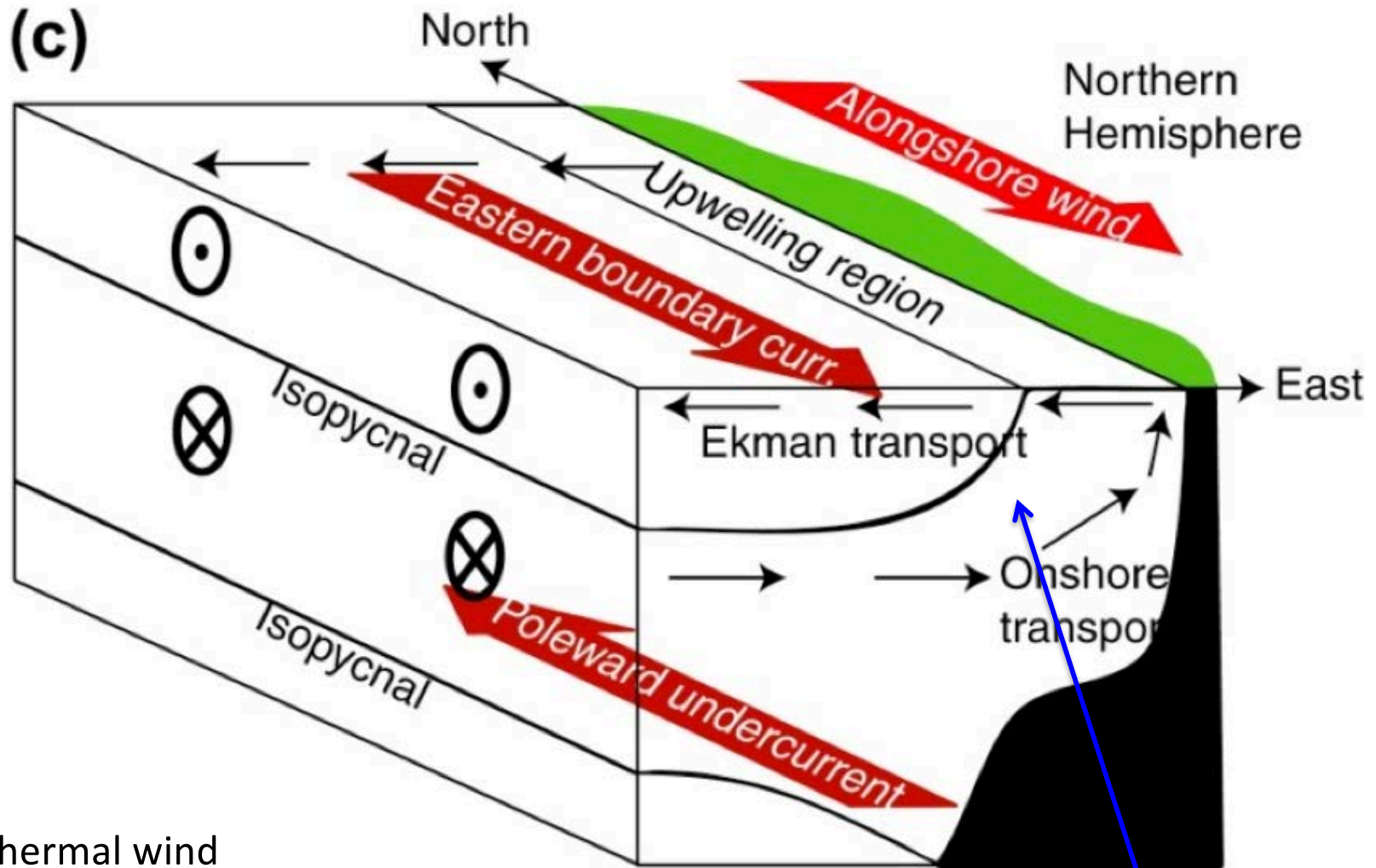


# Eastern boundary current system





# Coastal Ekman upwelling

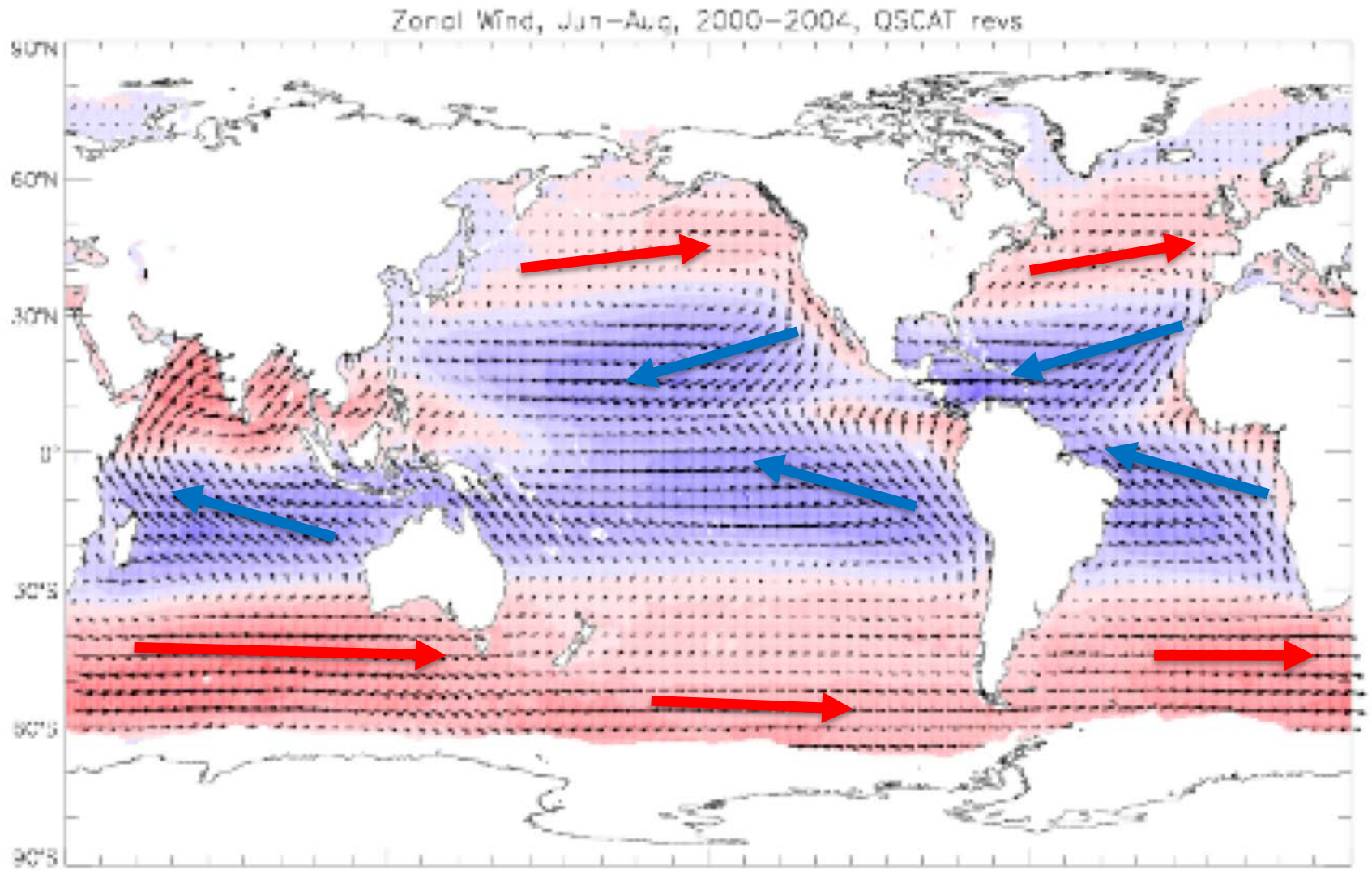


Thermal wind

$$\frac{\partial v_g}{\partial z} = -\frac{g}{f\rho} \frac{\partial \rho}{\partial x}$$

Density gradient  $\frac{\partial \rho}{\partial x} > 0$

# Observed wind stress



Blue = westward (trade wind)

Red = eastward (westerly wind)

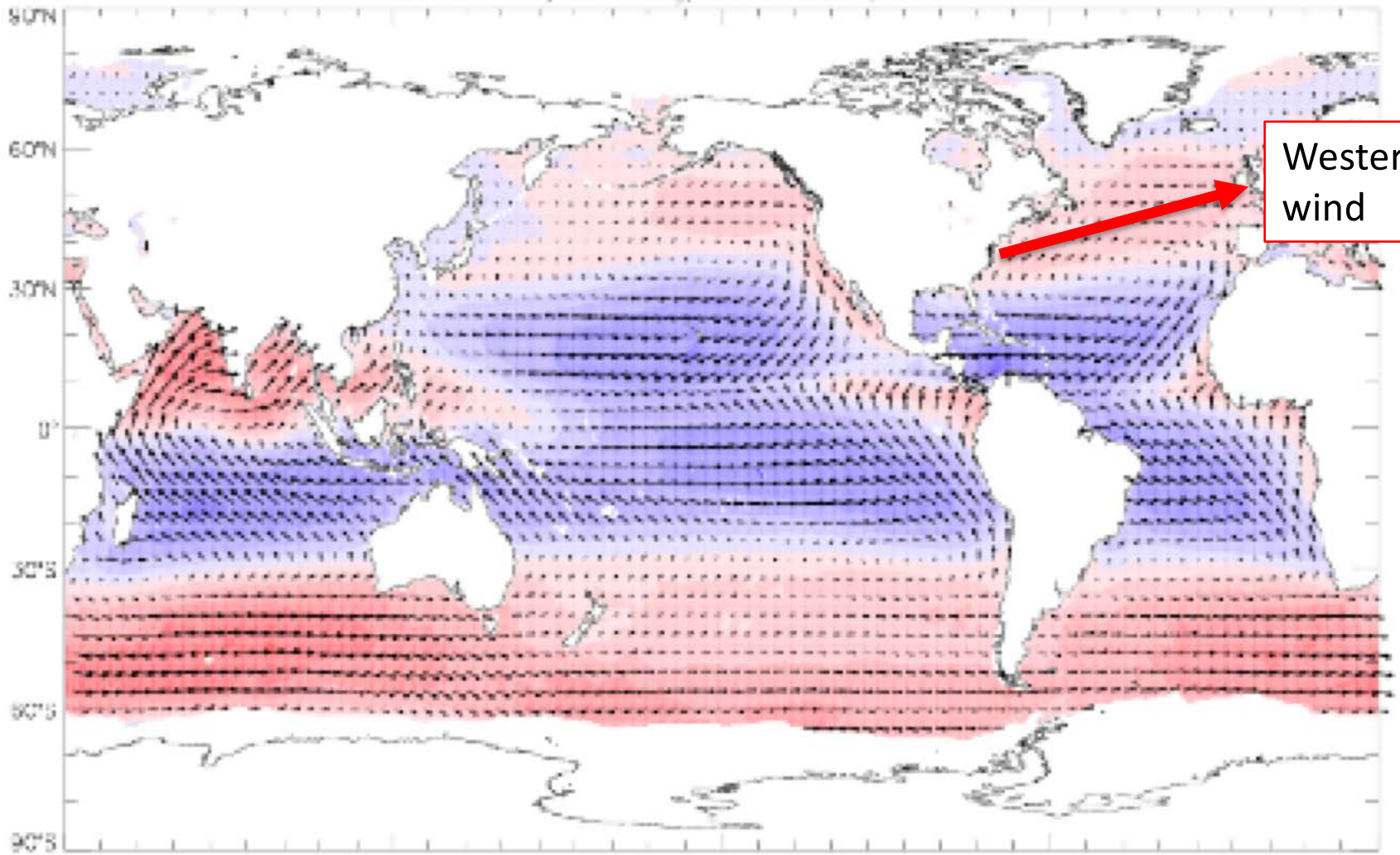
Cl = 2 m/s Min = -16.22 Max = 16.60





# Observed surface wind stress

Zonal Wind, Jun-Aug, 2000-2004, QSCAT revs



Westerly wind

Blue = westward (trade wind)

Red = eastward (westerly wind)

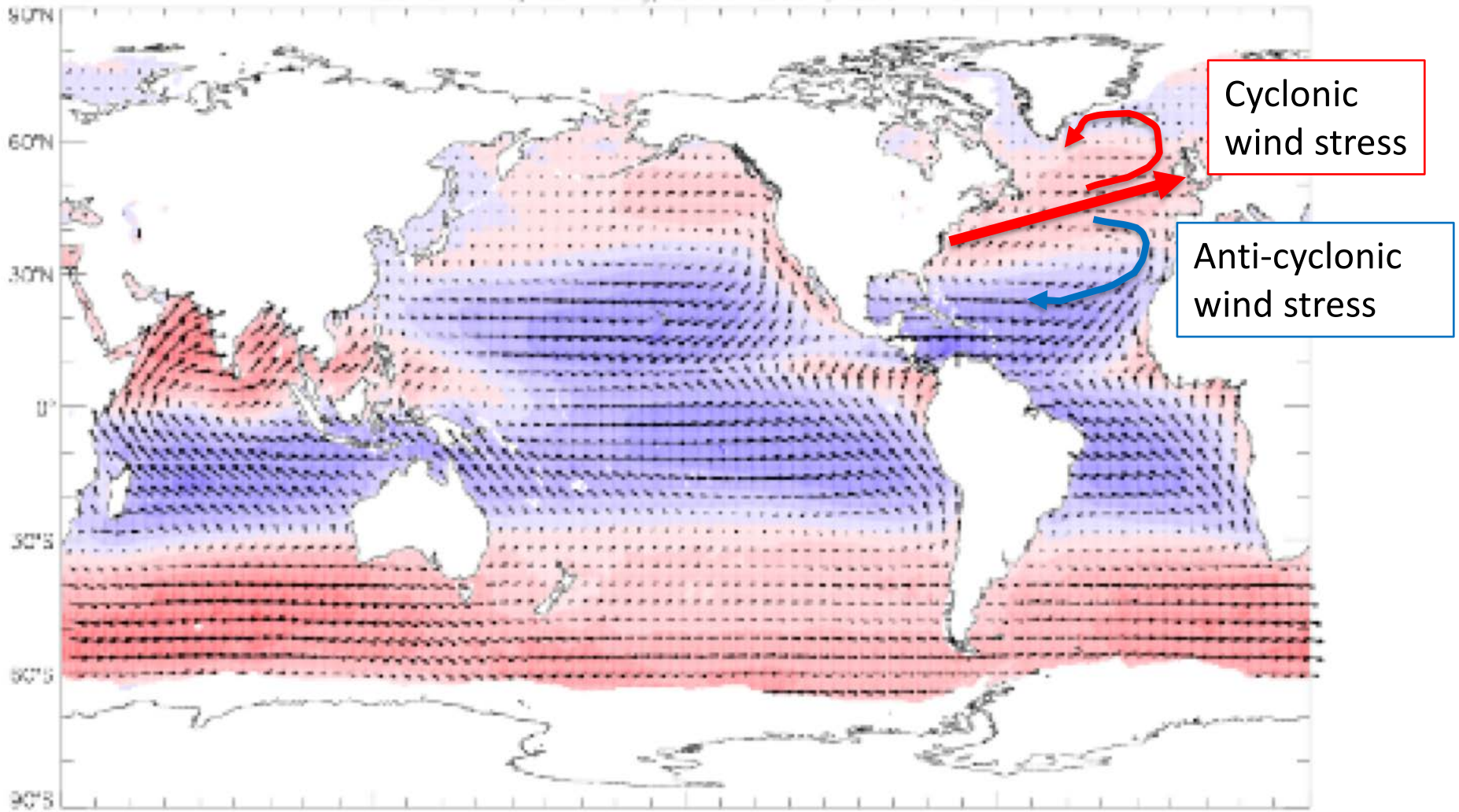
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# Observed surface wind stress

Zonal Wind, Jun-Aug, 2000-2004, QSCAT revs



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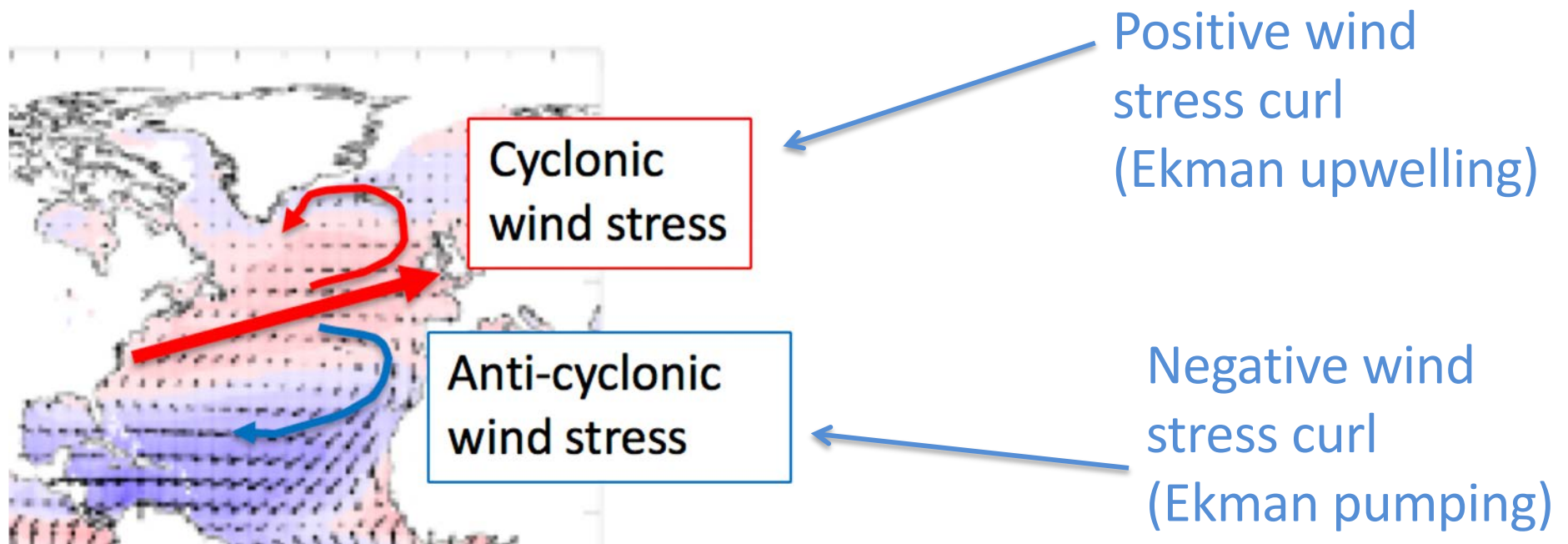
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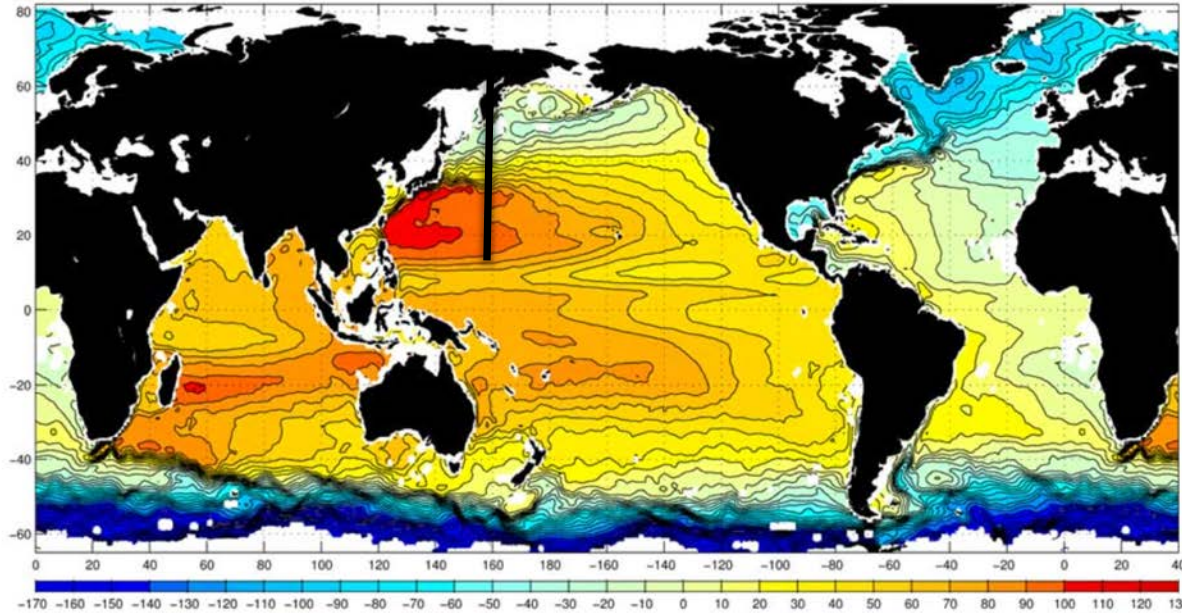
# Wind stress curl

- **Wind stress curl** measures the spin of the wind stress
  - Use your right hand
  - Counter clockwise = thumb up = positive curl
  - Clockwise = thumb down = negative curl
  - Vertical velocity depends on the wind stress curl



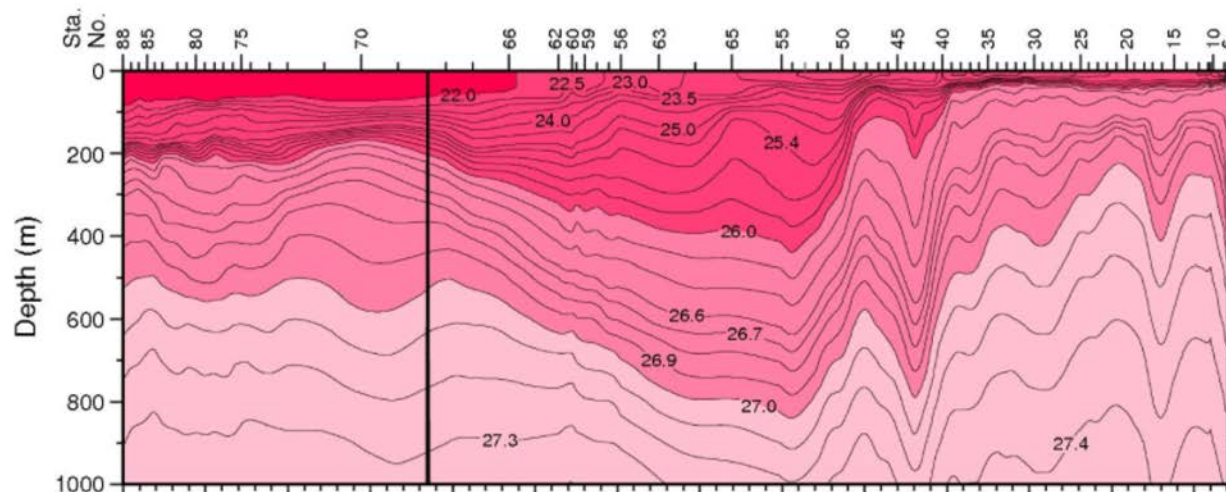


# Effect of Ekman upwelling/downwelling on the ocean density structure



The high SSH of the western subtropics is reflected in the deep thermocline (i.e. high steric height).

**Figure 1.** 1992–2002 mean absolute sea level  $\eta_0$  obtained as described in this paper. Contour interval is 10 cm. Sea level is computed from the values of  $\nabla\langle\eta\rangle$  estimated according to (2) on  $1^\circ$  spatial grid with the condition of zero global mean.



# Wind-driven gyres

- Ekman flow is only active in top 20-30m of the ocean.
- Geostrophic circulation extends much deeper depths, over several hundreds of meters.
- → Ekman upwelling/downwelling can drive the horizontal geostrophic circulation.

# 1947: Sverdrup balance

- Consider 3-way balance between Coriolis, pressure gradient and frictional forces

$$-fv = -\frac{1}{\rho_0} \frac{\partial p}{\partial x} + \frac{1}{\rho_0} \frac{\partial \tau_x}{\partial z}$$

$$fu = -\frac{1}{\rho_0} \frac{\partial p}{\partial y} + \frac{1}{\rho_0} \frac{\partial \tau_y}{\partial z}$$

# Sverdrup balance

- Consider 3-way balance between Coriolis, pressure gradient and frictional forces

$$-\frac{\partial}{\partial y} : -fv = -\frac{1}{\rho_0} \frac{\partial p}{\partial x} + \frac{1}{\rho_0} \frac{\partial \tau_x}{\partial z}$$

$$+\frac{\partial}{\partial x} : fu = -\frac{1}{\rho_0} \frac{\partial p}{\partial y} + \frac{1}{\rho_0} \frac{\partial \tau_y}{\partial z}$$

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$$f \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + \beta v = \frac{1}{\rho_0} \frac{\partial}{\partial z} \left( \frac{\partial \tau_y}{\partial x} - \frac{\partial \tau_x}{\partial y} \right)$$

# Theory for the ocean gyres

- Integrating from top to bottom of the ocean,

$$\beta V_s = \frac{1}{\rho_0} \left( \frac{\partial \tau_y}{\partial x} - \frac{\partial \tau_x}{\partial y} \right)$$

Northward motion  
leads to increased  
planetary spin

Curl of the wind stress  
The input of spin by the  
wind

Positive (negative) wind stress curl  $\rightarrow$  northward (southward)  
motion for water column

# The beta ( $\beta$ ) effect

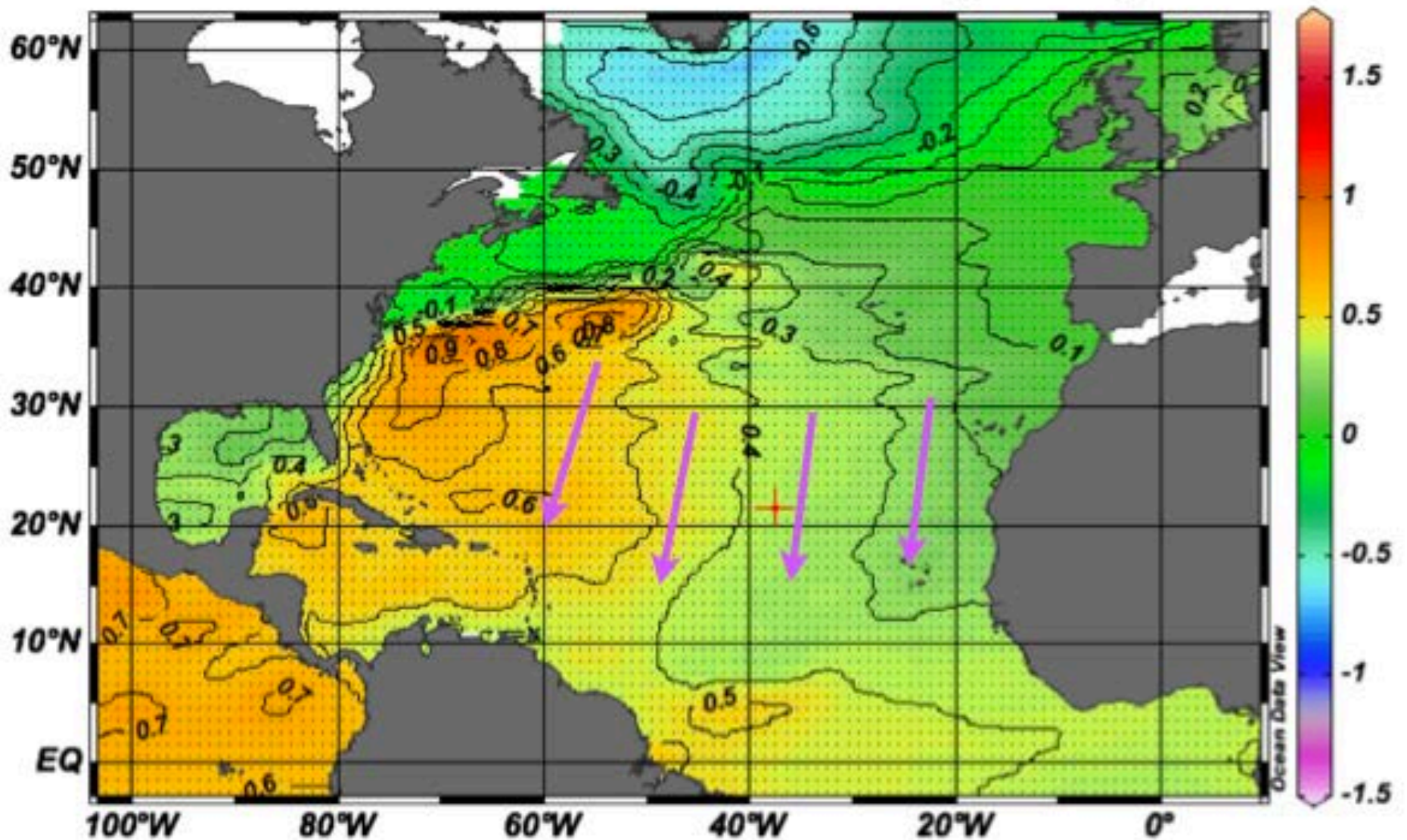
- Coriolis parameter changes with latitude.  
 $df/dy = \beta$ .
- The  $\beta$  effect has profound influence on geophysical fluid dynamics.
- One of the examples is the ocean gyres where the spin of wind stress drives horizontal (north-south) motion.



# Vorticity (spin) balance

- Wind stress can introduce spin into the ocean.
- Fluid can spin up/down (relative vorticity)
- Coriolis parameter ( $f$ ) measures the planetary spin (planetary vorticity)
- $f$  increases poleward. Thus, poleward motion increases its planetary spin.

# SSH fields: southward interior flow



# Issues with Sverdrup circulation

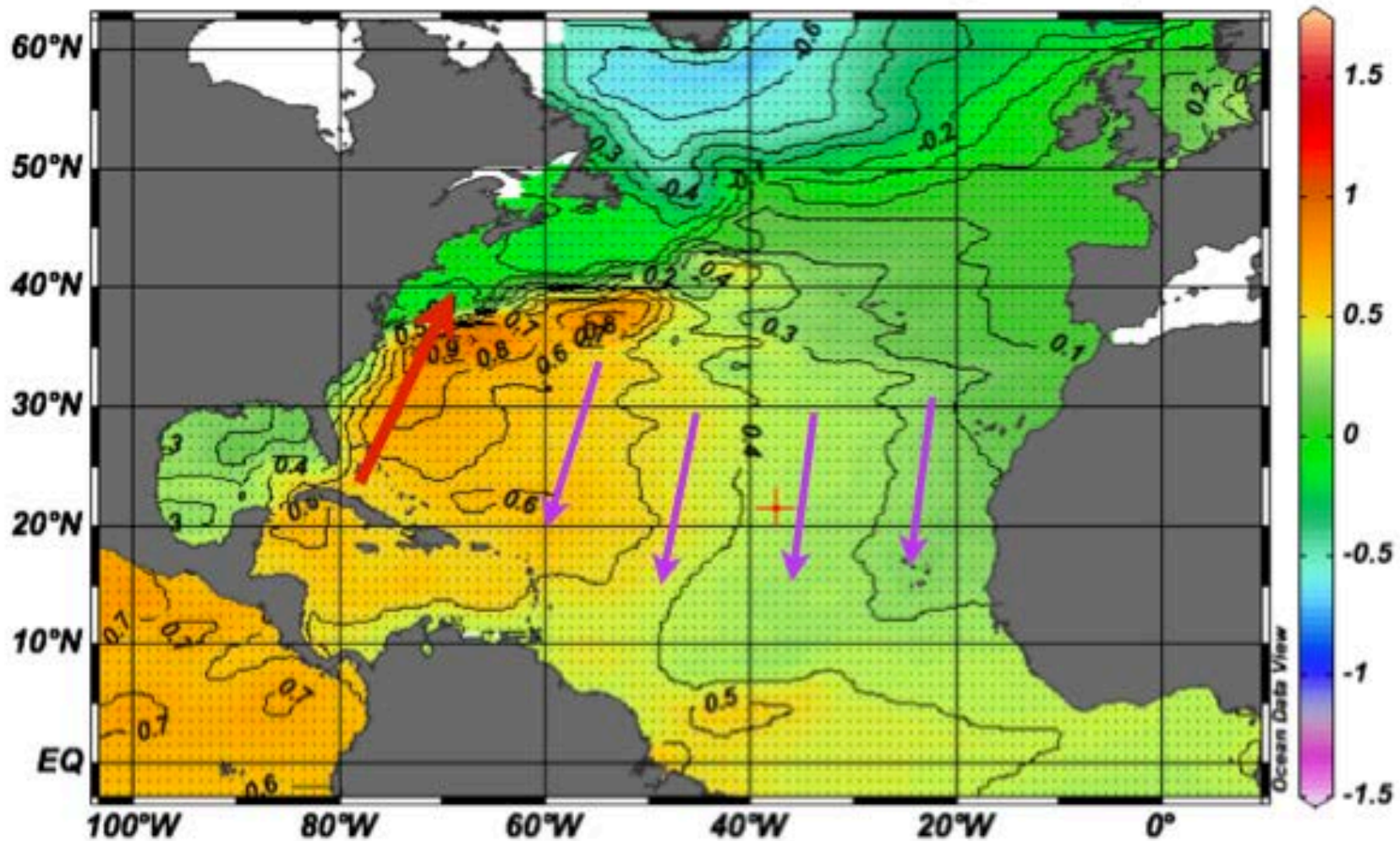
- Sverdrup circulation is equatorward everywhere in the subtropics (wind stress curl  $< 0$ )
- Does not conserve mass (poleward return flow is required)

# 1948

- H. Stommel developed the theory for the western boundary current, followed by Munk (1950) and Fofonoff (1954).

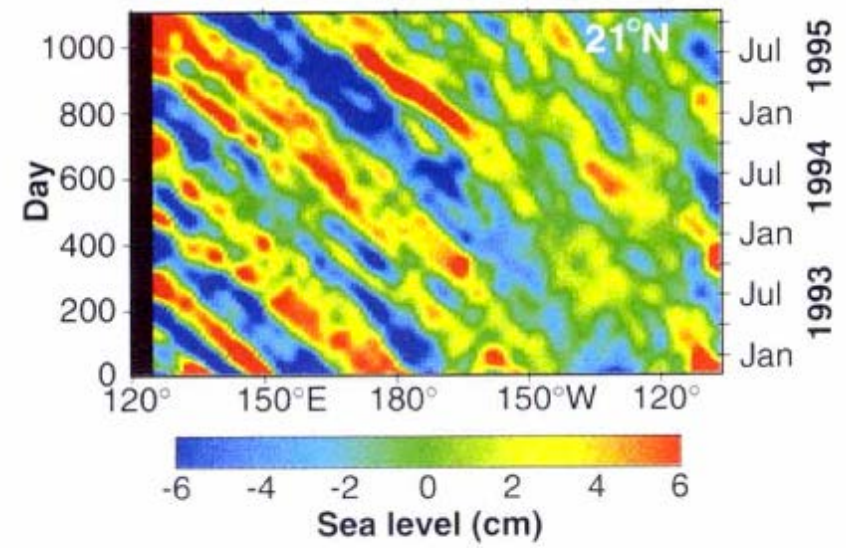
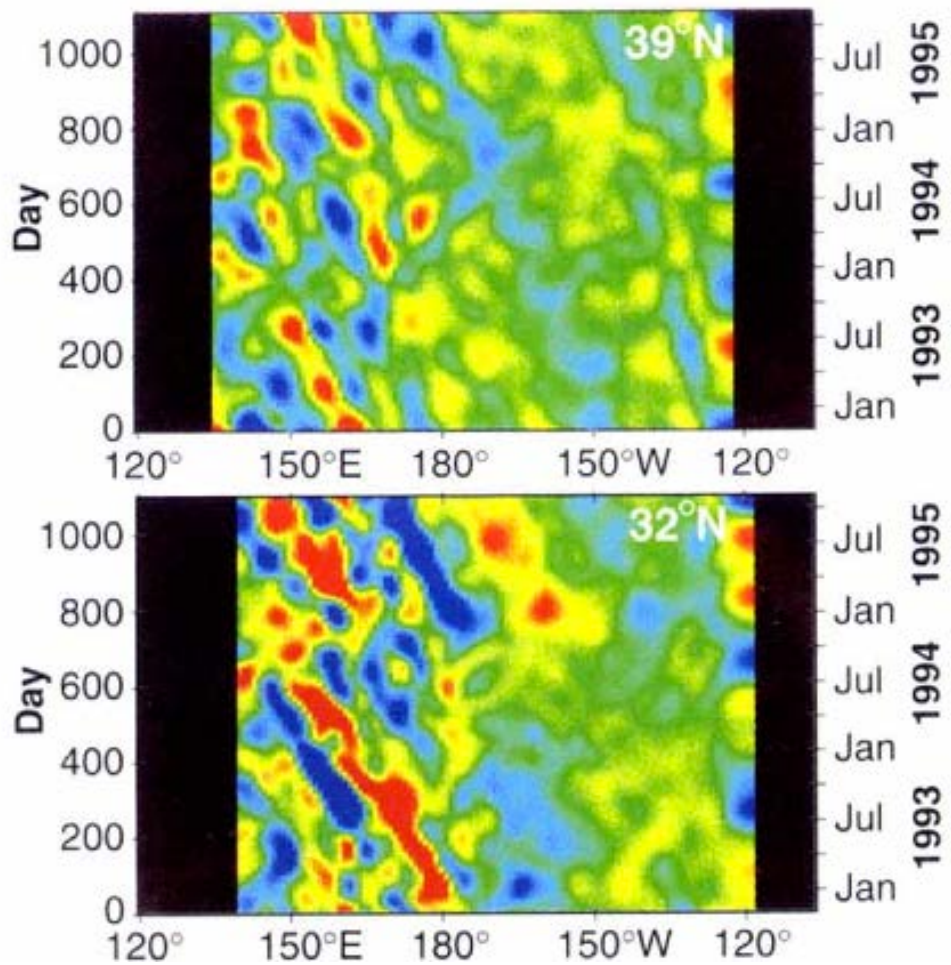
# Western boundary current

- Northward return pathway for the Sverdrup circulation





# Rossby waves (as observed by satellite SSH)



**Fig. 2.** Time-longitude sections of filtered sea level (22) in the Pacific Ocean along 39°, 32°, and 21°N. These examples are representative of extratropical latitudes throughout the world ocean.

Chelton and Schlax (1996) Science

Rossby wave propagates westward. It also transfers large scale energy to the west.

# Subtropical gyre circulation

- Atmosphere applies negative wind curl (clockwise spin) over the subtropical NH oceans
  - Transient response: Rossby waves are excited, transferring the spin (energy) towards the western boundary
  - Frictional dissipation at the western boundary is the ultimate sink of the spin (energy)
- Steady response: Sverdrup circulation transports mass southward, which is balanced by the northward western boundary current